## Module 8 - Bike Rite Kickstarter Campaign

## Background

Kickstarter (http://www.kickstarter.com/) is a popular crowdfunding site that was launched in 2009. Kickstarter was originally conceived to help artists raise funds to finance creative projects (e.g., films, works of art, performances). Many of the projects on Kickstarter still relate to the arts, but others are projects to raise money for new products or for new service businesses.

When an entrepreneur or artist starts a Kickstarter campaign, he or she sets the fundraising goal, the funding period (defined by a start date and an end date), and the awards set for different levels of funding pledges. For example, someone who is running a Kickstarter campaign to fund the production of a documentary might offer "a thank you in the credits" to anyone who pledges $\$ 20$ or more. To see some examples of award levels, go to the Kickstarter site and look at some examples of projects.

NOTE that if a campaign does not reach its fundraising goal, no pledged money can be collected.

Sarah and Matt are two friends who have been working on an idea for a uniquely designed bicycle accessory used to mount a cell phone on the handlebars, BikeRite ${ }^{1}$. They have decided to run a Kickstarter campaign to raise the money they need for initial production, distribution, and marketing. They don't want to set the fundraising goal too high. If they don't meet it, then they wouldn't collect any of the money pledged. They also don't want to set it too low and miss out on some money. To help inform their decision about the fundraising goal, they found a blog that had collected and posted several years' worth of data on Kickstarter projects (over 30,000 of them). They need to discuss two of their decisions: what should their Kickstarter fundraising goal be, and what award levels should they offer?

The Excel workbook for this module consists of 3 tabs.

1. The "Database" tab is raw data downloaded from http://blog.thingswestart.com/our-data/. Each row in the data set is a project. For each project, there are many details, including "goal" (the fundraising goal) and "pledged" (the total amount backers committed to give if the fundraising goal is met). Projects are also organized into a "category" (e.g., Narrative Film) and a "category_parent" (e.g., Film \& Video).
2. The "List of Comparables" tab contains specific data for twelve comparable projects that were also for bicycle accessories. For each comparable project, the data shows up to ten pledge levels, and for each of the pledge levels used in the project, there is a column showing the number of backers at that level.
3. The "Pricing Research" tab displays a summary of the pricing research that is referred to in Part 4.
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## Part 0: Probability Distribution and Expected Value

A probability distribution summarizes the outcomes and corresponding likelihood of each outcome. Using a concept similar to a weighted mean, the average or expected value of the probability distribution can be computed.

1) To begin this Module, view the screencast Expected Value.

## Part 1: Project Data

1) How many total projects are in the data set?
2) How many of them reached their funding goal (i.e., had pledges that reached or exceeded the goal)? What percentage of all the projects reached their funding goal?
3) There are four years of data: 2012, 2013, 2014, and 2015. What percentage of projects in the data set reached their funding goal each year? (Use the ending date to determine the year of the project.)

| Year (of End Date) | \% of Projects that <br> Reached Funding Goal |
| :---: | :---: |
| 2012 | $59.27 \%$ |
| 2013 | $62.09 \%$ |
| 2014 |  |
| 2015 |  |

4) Is the average of the four percentages in the table above equal to the percentage from question 2) (the percentage of all projects that reached their funding goal)? Why or why not?
5) What percentage of all projects under the Crafts category parent reached their funding goal?

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6) Did a higher percentage of projects under the Video Games category or the Jazz category reach their funding goal?
7) What percentage of all projects under the Art category parent ending in 2012 reached their funding goal?
8) Using all projects in the data set,
a. How many projects had a goal of $\$ 50,000$ or lower?
b. What percentage of the projects with goals of $\$ 50,000$ or lower reached their funding goal?
c. Fill in the missing cells in the following table, using all the projects in the database.

Projects that meet their goal collect the pledged amount. Projects that do not meet their goal collect no funds. Calculate the Average Funds Collected: the average amount of money collected per project, including projects that collect nothing because they did not meet their goal.

| Goal Level | Number of <br> Projects | \% Reached <br> Funding Goal | Average Funds <br> Collected |
| :---: | :---: | :---: | :---: |
| $\$ 0-\$ 10,000$ | 62,929 | $53.21 \%$ | $\$ 3,671.37$ |
| $\$ 10,000.01-\$ 20,000$ |  |  |  |
| $\$ 20,000.01-\$ 30,000$ |  |  | $\$ 21,682.75$ |
| $\$ 30,000.01-\$ 40,000$ | 2,141 |  |  |
| $\$ 40,000.01-\$ 50,000$ |  | $29.74 \%$ |  |

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d. Fill in the missing cells in the following table, using just the projects under the Design category parent.

| Goal Level | Number of <br> Projects | \% Reached <br> Funding Goal | Average Funds <br> Collected |
| :---: | :---: | :---: | :---: |
| $\$ 0-\$ 10,000$ | 2,055 | $68.86 \%$ | $\$ 14,401.92$ |
| $\$ 10,000.01-\$ 20,000$ |  |  | $\$ 47,294.35$ |
| $\$ 20,000.01-\$ 30,000$ | 113 |  |  |
| $\$ 30,000.01-\$ 40,000$ |  | $83.70 \%$ |  |
| $\$ 40,000.01-\$ 50,000$ |  |  | $\$ 252,413.27$ |

e. From this data, can you conclude that projects with higher goals (up to $\$ 50,000$ ) tend to collect more money?

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## Part 2: Setting Levels

Setting the award levels is an important part of a Kickstarter campaign. Backers (people who pledge to support the campaign) choose a level at which to contribute, and the project owners provide an award at each level. For new products, some of the award levels usually involve pre-sales of the product.

For example, here are the levels for a Bicycle Bell project (project 12) that was funded on Kickstarter (https://www.kickstarter.com/projects/139160027/a-better-bicycle-bell-made-in-the-usa):

- Pledge \$1: "Thanks!"
- Pledge $\$ 35$ or more: a bell in the raw metal color
- Pledge $\$ 45$ or more: a bell in black
- Pledge $\$ 55$ or more: a polished metal bell
- Pledge $\$ 80$ or more: two bells, one raw and one black

1) Looking at the data for the Bicycle Bell project on the List of Comparables tab, find the percentage of backers that pledged at each of the five levels. Fill in the missing cells in the following table.

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| Pledge <br> Level | Number of Backers | \% of Total Backers for the <br> Project |
| :---: | :---: | :---: |
| $\$ 1$ | 86 | $1.48 \%$ |
| $\$ 35$ | 2151 |  |
| $\$ 45$ |  |  |
| $\$ 55$ |  | $29.82 \%$ |
| $\$ 80$ |  |  |

Sarah and Matt decide that they are going to use the same pledge levels with similar awards for their campaign.
2) If Sarah and Matt can attract 500 backers in total, and the backers pledge in the same proportions per level as they did for the Bicycle Bell project, how much money would Sarah and Matt raise? (For this question, assume that if someone pledges at a level (say \$45), they contribute exactly at that level, not more. Also, in using the proportions, don't round the number of backers at each level to whole numbers.)
3) Create a graph in Excel of the estimated money pledged as a function of the number of backers for Sarah and Matt's project. Use a range of 0 to 2000 backers in your graph.
a. Does your graph show a straight line?
b. If so, what is the slope of the line? What is the meaning of that slope? If not, how can you explain the shape of the graph?
4) Write the equation, by hand, for the function shown in your graph in Question 4.
5) If the fundraising goal is set at $\$ 20,000$, how many backers do Sarah and Matt need to meet that goal? Get your answer three ways and confirm that they are all the same:
a. Solve the written equation from question 4) to find an exact answer.
b. Use the graph you created in question 3) above to estimate the answer.
c. Numerically check your answer in your spreadsheet to see if the number of backers you found does, in fact, yield \$20,000.
6) Looking at the data for the Bicycle Bell project (on the List of Comparables tab), you see that the reported amount pledged (in the column labeled Pledged) was $\$ 331,938$.

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a. If backers at each level in that project simply pledged the minimum for that level and no more, how much would have been pledged in total? (To further clarify: assume the 2151 backers who pledged at the \$35 level each pledged exactly \$35.)
b. In aggregate, by what percentage did the Bicycle Bell backers pledge more than the minimum at each level? That is, if the pledge level was $\$ 15$ and backers pledged $\$ 18$, they would be pledging $20 \%$ more than the minimum at that level. You don't have the individual pledges, but you have the total pledged (in the Pledged column) as well as the number of backers at each level. You can calculate the aggregate percentage above the minimum from that data.
c. Sarah and Matt consider the possibility that backers will pledge above the minimum for each level for their project too. If backers pledge above the minimum at each level at the same aggregate percentage as the Bicycle Bell project, then how many backers would they need to meet a $\$ 20,000$ fundraising goal?

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## Part 3: Capital Expenditure

If Sarah and Matt raise enough money, they can afford to invest in production equipment that would save them money over the lifetime of their business, assuming they realize at least moderate success.

They face a trade-off in production costs: they can invest more upfront for a lower per-unit cost, or less upfront for a higher per-unit cost. In particular, they have an option to purchase a custom mold that would allow production via a more automated, injection-molding production process.

- The custom mold costs $\$ 15,000$ and lasts a long time. Once that mold is created, the per-unit cost of producing each unit is $\$ 0.50$.
- If they don't create the mold, they need to buy other equipment for $\$ 500$, and the more laborintensive process costs $\$ 5$ per unit.

If they only end up making a small number of units, buying the custom mold would not be worth it. For example, for 100 units, with the custom mold, they would spend $\$ 15,000+100$ * ( $\$ 0.50$ ) = \$15,050 . But with the other approach, they would spend only $\$ 500+100$ * (\$5)=\$1,000.

1) What is the breakeven number of units at which the custom mold is the better choice? That is, how many units would they have to produce to make the custom mold a lower cost option? Write the equation on paper and solve it.
2) Create a graph in Excel that shows the total cost under each of the two production processes (custom mold vs. more labor-intensive) as a function of the number of units produced. For number of units produced, use a range of 0 to 6,000. Label your graph to show the answer you got for question 1).
3) Confirm the solution to your equation in question 1) works in your spreadsheet.
4) Using the pledge levels from Part 2 and the proportions of backers at each level from the Bicycle Bell project (and once again assuming that backers pledge the minimum at each pledge level), answer the following question. How many backers do they need to cover the upfront cost (the $\$ 15,000$ ) for the custom mold?

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## Part 4: Pricing

If Sarah and Matt are able to raise the money and get their product produced, they are thinking that they will charge $\$ 30-\$ 70$ for it, which is a middle-of-the-pack price for their product category. It won't be the cheapest, and it won't be the most expensive. They think people will want to buy it because of the unique design.

They did a little market research on the pricing using a survey. The survey showed people a description of the product and a price, and then asked, "How likely would you be to purchase this new product at this price?" The survey respondents were people who regularly ride bicycles. They tested five price points (but each survey respondent saw only one price point). Below (and on the tab called Pricing Research), you see a summary of the relevant responses.

| Price Point | Percent of people surveyed who said they would "probably" or "definitely" buy |
| :---: | :---: |
| $\$ 30$ | $16.25 \%$ |
| $\$ 40$ | $12.00 \%$ |
| $\$ 50$ | $8.75 \%$ |
| $\$ 60$ | $3.00 \%$ |
| $\$ 70$ | $3.05 \%$ |

1) Assume the product will be available in stores and 100000 regular bike riders will be aware of it. Using the percentages in the chart above as purchase percentages, create a graph that shows the amount of revenue at each of the price points.
2) If 200000 (instead of 100000) regular bike riders will be aware of the product, does that change the revenue graph? Does it change the revenue-maximizing price? If so, how? If not, why not?
3) If Sarah and Matt choose the custom-mold production process (as described in Part 3), then of the price points considered, which one maximizes profit? (Profit is revenue minus cost.)

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4) If Sarah and Matt choose the labor-intensive production process (as described in Part 3), then of the price points considered, which one maximizes profit?

## Part 5: Larger Pledges

In the Bicycle Bell project that Sarah and Matt used as a model, the highest pledge level amount was only $\$ 80$. However, some of the other comparable projects had pledge levels much higher than that.

1) Looking on the List of Comparables tab, what was the highest pledge level amount offered out of the projects listed?

How many people pledged at that level?
2) How many of the 12 comparable projects offered pledge levels at $\$ 100$ or higher? Considering all the backers of all 12 projects, what percent of them pledged at a pledge level of $\$ 100$ or higher?
3) Sarah and Matt are considering offering a higher pledge level in addition to the five lower pledge levels from the Bicycle Bell project. They are considering a $\$ 250$ pledge level and make the following assumptions:

- They will have at most three backers.
- The probability of getting at least one backer at this level is the same as the percentage of all backers of all 12 projects at $\$ 100$ or higher (found in question 2).
- The probability of getting exactly one backer at $\$ 250$ is twice the probability of getting exactly two backers at $\$ 250$.
- The probability of getting exactly three backers at $\$ 250$ is equal to the probability of getting exactly 2 backers at $\$ 250$

Using this information:
i. What is the probability that they have 0 backers at $\$ 250$ ?
ii. What is the probability that they have exactly 1 backer at $\$ 250$ ?
iii. What is the probability that they have exactly 2 backers at $\$ 250$ ?

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iv. What is the probability that they have exactly 3 backers at $\$ 250$ ?
b. Assume that any backers at the highest level ( $\$ 250$ ) are independent of what happens at the five lower levels. What is the "expected value" of the total money pledged at the \$250 level?

An "expected value" is a probability-weighted average of values. Assume that people that pledge at that level pledge exactly $\$ 250$, not more.

## Part 6: Analyzing Base-Case, Pessimistic, and Optimistic Scenarios

In Part 2, Question 2, you computed an estimate of money pledged for the Bicycle Bell Product with 500 backers. Use that as a base-case scenario, or most likely scenario. Sarah and Matt are also considering a pessimistic scenario, with only 200 backers, and an optimistic scenario, with 1,200 backers. They assume that the proportions of people who would participate at the different pledge levels would stay the same across the base-case, pessimistic, and optimistic scenarios. (As before, don't round the number of backers at each level to whole numbers.)

For the questions below, use only the initial pledge levels (\$1-\$80), not the higher (\$250) pledge level.

1) Pessimistic scenario.
a. Estimate the amount of money pledged under the pessimistic scenario.
b. Would they be able to afford the upfront cost of the custom-mold production process (see Part 3) in this scenario?
c. Which price should they charge (see Part 4) in this scenario?
2) Optimistic scenario.
a. Estimate the amount of money pledged under the optimistic scenario.
b. Would they be able to afford the upfront cost of the custom-mold production process (see Part 3) in this scenario?

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c. Which price should they charge (see Part 4) in this scenario?

- Sarah and Matt know that the three scenarios are just three cases of what could happen—of course there are many variations on the outcomes. But as an approximation to help them think through both possible outcomes and their likelihoods, they estimate probabilities for each of the three cases.


## They assign a

- $60 \%$ chance to the base scenario,
- $20 \%$ chance to the pessimistic, and a
- $20 \%$ chance to the optimistic scenario.

If the funding goal is set at $\$ 12,000$, what is the expected value (using the scenario probabilities) of money they would collect?

## Selected Answers

## Part 1

1) 90,122 projects
2) 43,420 projects reached their funding goal; $48.18 \%$
3) No, because the average of the four percentages does not take into account the number of projects for each year. For instance, if one year has more projects than another, then its \% should affect the average more.
4) $25.06 \%$
5) Jazz (62.88\%) had a higher percentage than Video Games (52.05\%).
6) $50.83 \%$
7) a) 84,134 projects had a goal of $\$ 50,000$ or lower; b) $50.17 \%$

Part 2
2) $\$ 25,751.60$ with 500 backers

3)

3b) Slope = \$51.50, the average amount pledged per backer.
4) $y=51.5 x$
5) About 388.3 backers
6) a) $\$ 298,461$; b) $11.22 \%$ more than the minimum; c) 349.2 backers

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## Part 3

1) 3222.22 units. For 3223 or more units, the custom mold option has a lower total cost.

2) 
3) About 292 backers

Part 4
1)

2) The number of riders aware of the product will change the total revenue, but the shape of the graph will remain the same, so the revenue-maximizing price will not change.
3) $\$ 30$ will earn the greatest profit $(\$ 464,375)$.
4) $\$ 40$ will earn the greatest profit $(\$ 419,500)$.

## Part 5

1) The greatest pledge level was $\$ 6,000$. The number of backers who pledged at that level was 1.
2) 11 of the 12 projects; $4.82 \%$ of the backers.
3) a)i. $95.18 \%$; a)ii. $2.41 \%$; a)iii. $1.21 \%$; a)iv. $1.21 \%$; b) $\$ 21.09$

## Part 6

1) a) $\$ 10,300.64$; b) They cannot afford the custom mold.; c) $\$ 40$ (optimal for labor-intensive process)

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2) a) $\$ 61,803.83$; b) They can afford the custom mold.; c) $\$ 30$ (optimal for mold process) 3) $\$ 27,811.72$

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[^0]:    ${ }^{1}$ BikeRite is a fictitious but realistic project, based on similar Kickstarter projects.

